## Probability - AS Mathematics P2

1. June/2022/Paper_7356/02/No. 14

Yingtai visits her local gym regularly.
After each visit she chooses one item to eat from the gym's cafe.
This could be an apple, a banana or a piece of cake.
She chooses the item independently each time.
The probability that Yingtai chooses each of these items on any visit is given by:

$$
\begin{aligned}
\mathrm{P}(\text { Apple }) & =0.2 \\
\mathrm{P}(\text { Banana }) & =0.35 \\
\mathrm{P}(\text { Cake }) & =0.45
\end{aligned}
$$

For any four randomly selected visits to the gym, find the probability that Yingtai chose:
(a) at least one banana.
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$\qquad$
(b) the same item each time.
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$\qquad$
(c) apple twice and cake twice.
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2. June/2022/Paper_7356/02/No. 15

The discrete random variable $X$ is modelled by the probability distribution defined by:

$$
\mathrm{P}(X=x)=\left\{\begin{array}{cc}
c x & x=1,2 \\
k x^{2} & x=3,4 \\
0 & \text { otherwise }
\end{array}\right.
$$

where $k$ and $c$ are constants.
(a) State, in terms of $k$, the probability that $X=3$
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$\qquad$
$\qquad$
(b) Given that $\mathrm{P}(X \geq 3)=3 \times \mathrm{P}(X \leq 2)$

Find the exact value of $k$ and the exact value of $c$.
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