## Matrices - A2 Further Mathematics P1

1. June/2022/Paper_7367/01/No. 4

The vector $\mathbf{v}$ is an eigenvector of the matrix $\mathbf{N}$ with corresponding eigenvalue 4

The vector $\mathbf{v}$ is also an eigenvector of the matrix $\mathbf{M}$ with corresponding eigenvalue 3

Given that

$$
\mathbf{N M}^{2} \mathbf{v}=\lambda \mathbf{v}
$$

find the value of $\lambda$
Circle your answer.
2. June/2022/Paper_7367/01/No. 7

The matrix $\mathbf{M}$ is defined as

$$
\mathbf{M}=\left[\begin{array}{ccc}
1 & 7 & -3 \\
3 & 6 & k+1 \\
1 & 3 & 2
\end{array}\right]
$$

where $k$ is a constant.
(a) (i) Given that $\mathbf{M}$ is a non-singular matrix, find $\mathbf{M}^{-1}$ in terms of $k$
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(a) (ii) State any restrictions on the value of $k$
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$\qquad$
(b) Using your answer to part (a)(i), solve

$$
\begin{array}{r}
x+7 y-3 z=6 \\
3 x+6 y+6 z=3 \\
x+3 y+2 z=1
\end{array}
$$

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