## Exponentials and logarithms - A2 Mathematics P3

1. June/2022/Paper_7357/03/No. 7

A planet takes $T$ days to complete one orbit of the Sun.
$T$ is known to be related to the planet's average distance $d$, in millions of kilometres, from the Sun.

A graph of $\log _{10} T$ against $\log _{10} d$ is shown with data for Mercury and Uranus labelled.

(a) (i) Find the equation of the straight line in the form

$$
\log _{10} T=a+b \log _{10} d
$$

where $a$ and $b$ are constants to be found.
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$\qquad$
(a) (ii) Show that

$$
T=\mathrm{K} d^{\mathrm{n}}
$$

where K and n are constants to be found.
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$\qquad$
(b) Neptune takes approximately 60000 days to complete one orbit of the Sun.

Use your answer to 7(a)(ii) to find an estimate for the average distance of Neptune from the Sun.
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