AQA – Further vectors – AS Further Mathematics P1

1. June/2021/Paper_7366/1/No.5

Show that the vectors
$$\begin{bmatrix} 1 \\ -3 \\ 5 \end{bmatrix}$$
 and $\begin{bmatrix} 7 \\ 4 \\ 1 \end{bmatrix}$ are perpendicular.

[2 marks]

2. June/2021/Paper_7366/1/No.15

Two submarines are travelling on different straight lines.

The two lines are described by the equations

$$\mathbf{r} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix} + \lambda \begin{bmatrix} 5 \\ 3 \\ -2 \end{bmatrix} \quad \text{and} \quad \frac{x-5}{4} = \frac{y}{2} = 4 - z$$

(a) (i) Show that the two lines intersect.

[3 marks]

(a) (ii) Find the position vector of the point of intersection.

[1 mark]

(b) Tracey says that the submarines will collide because there is a common point on the two lines.

Explain why Tracey is not necessarily correct.

[1 mark]

(c) Calculate the acute angle between the lines

$$\mathbf{r} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix} + \lambda \begin{bmatrix} 5 \\ 3 \\ -2 \end{bmatrix} \quad \text{and} \quad \frac{x-5}{4} = \frac{y}{2} = 4 - z$$

Give your angle to the nearest $0.1^{\circ}\,$

[3 marks]