## AQA - Exponentials and logarithms - AS Mathematics P1

1. June/2021/Paper_7356/1/No. 7

Scientists observed a colony of seabirds over a period of 10 years starting in 2010.
They concluded that the number of birds in the colony, its population $P$, could be modelled by a formula of the form

$$
P=a\left(10^{b t}\right)
$$

where $t$ is the time in years after 2010, and $a$ and $b$ are constants.
(a) Explain what the value of $a$ represents.
(b) Show that $\log _{10} P=b t+\log _{10} a$
(c) The table below contains some data collected by the scientists.

| Year | $\mathbf{2 0 1 3}$ | $\mathbf{2 0 1 5}$ |
| :---: | :---: | :---: |
| $t$ | 3 |  |
| $P$ | 10200 | 12800 |
| $\log _{10} P$ | 4.0086 |  |

(c) (i) Complete the table, giving the $\log _{10} P$ value to 5 significant figures.
(c) (ii) Use the data to calculate the value of $a$ and the value of $b$.
(c) (iii) Use the model to estimate the population of the colony in 2024.
(d) (i) State an assumption that must be made in using the model to estimate the population of the colony in 2024.
(d) (ii) Hence comment, with a reason, on the reliability of your estimate made in part (c)(iii).

