AQA – Exponentials and logarithms – AS Mathematics P1

1. June/2021/Paper_7356/1/No.7

Scientists observed a colony of seabirds over a period of 10 years starting in 2010.

They concluded that the number of birds in the colony, its population P, could be modelled by a formula of the form

 $P = a(10^{bt})$

where t is the time in years after 2010, and a and b are constants.

(a) Explain what the value of *a* represents.

[1 mark]

(b) Show that $\log_{10} P = bt + \log_{10} a$

[2 marks]

(c) The table below contains some data collected by the scientists.

Year	2013	2015
t	3	
Р	10 200	12800
log ₁₀ P	4.0086	

(c) (i) Complete the table, giving the $\log_{10} P$ value to 5 significant figures.

[1 mark]

(c) (ii) Use the data to calculate the value of a and the value of b.

[4 marks]

(c) (iii) Use the model to estimate the population of the colony in 2024.

[2 marks]

(d) (i) State an assumption that must be made in using the model to estimate the population of the colony in 2024.

[1 mark]

(d) (ii) Hence comment, with a reason, on the reliability of your estimate made in part (c)(iii). [1 mark]