## AQA - Exponentials and logarithms - A2 Mathematics P2

1. June/2019/Paper_2/No. 8

Theresa bought a house on 2 January 1970 for $£ 8000$.
The house was valued by a local estate agent on the same date every 10 years up to 2010 .

The valuations are shown in the following table.

| Year | 1970 | 1980 | 1990 | 2000 | 2010 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Valuation price | $£ 8000$ | $£ 19000$ | $£ 36000$ | $£ 82000$ | $£ 205000$ |

The valuation price of the house can be modelled by the equation

$$
V=p q^{t}
$$

where $V$ pounds is the valuation price $t$ years after 2 January 1970 and $p$ and $q$ are constants.
(a) Show that $V=p q^{t}$ can be written as $\log _{10} V=\log _{10} p+t \log _{10} q$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) The values in the table of $\log _{10} V$ against $t$ have been plotted and a line of best fit has been drawn on the graph below.

| $t$ | 0 | 10 | 20 | 30 | 40 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\log _{10} V$ | 3.90 | 4.28 | 4.56 | 4.91 | 5.31 |



Using the given line of best fit, find estimates for the values of $p$ and $q$.
Give your answers correct to three significant figures.
[4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(c) Determine the year in which Theresa's house will first be worth half a million pounds.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(d) Explain whether your answer to part (c) is likely to be reliable.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

